

## Beam position monitor design for a third generation light source

Zhichu Chen,<sup>\*</sup> Yongbin Leng, Kairong Ye, Guobi Zhao, and Renxian Yuan<sup>†</sup>

Shanghai Institute of Applied Physics, Chinese Academy of Sciences, Shanghai 201800,  
China and Shanghai Synchrotron Radiation Facility, Chinese Academy of Sciences,  
Shanghai 201204, China

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The measurement of the beam orbit plays a very important role in particle accelerators. The button-type beam position monitor (BPM) was designed for the Shanghai Synchrotron Radiation Facility to reduce the impedances and to guarantee a high resolution of the measurement. Position resolution, beam impedance, higher-order mode, and impedance matching have been studied during the design based on the physical parameters of the storage ring at the Shanghai Synchrotron Radiation Facility. Meanwhile, an analytic formula of the BPM broadband impedance was derived based on a resistor-capacitor equivalent circuit. Thus, the impedance of the BPM could be analyzed quantitatively by simply measuring the capacitance of the electrode. This formula had been verified by comparing the results of the calculations of the formula and the simulations in MAFIA.

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### I. INTRODUCTION

The beam position monitor (BPM) system at the Shanghai Synchrotron Radiation Facility (SSRF) [1,2] provides beam orbit measurements with different beam position resolution properties depending on the integration time or bandwidth setting to ensure stable and effective operations for the orbit feedback system [3], the transverse feedback system [4], the tune measurement system [5,6], and the interlock system. For example, the orbit feedback system requires an information of the closed orbit of high resolution, in the range of  $1\ \mu\text{m}$  at a rate of approximately 1 ms, while the transverse feedback system needs bunch-by-bunch signals with a resolution in the order of  $10\ \mu\text{m}$  at a rate in the range of 2 ns. The tune measurement system requires turn-by-turn data with the resolution and data rate somewhere in between the previous two demands. The important technical challenges for the BPM electrodes design are beam impedance minimization, e.g., by suppression of beam excited higher-order modes (HOMs), and a good impedance matching, which will result in well-separated bunch-by-bunch signals with high signal-to-noise ratio (SNR). The following sections discuss various technical details in the BPM design, as well as beam and machine conditions at the SSRF.

### II. POSITION SENSITIVITY OF THE BPM PROBES

The electrodes of the BPM are usually fixed in the vacuum chamber, so the geometric layout of the vacuum chamber determines the layout of the BPM, except sizes and locations of the electrodes. Figure 1 illustrates the geometric layout of the BPM electrodes in the vacuum chamber of the storage ring at the SSRF. Pairs of electrodes ( $A$ - $B$  and  $C$ - $D$ ) were assembled as modules before being assembled symmetrically at the upper and lower surfaces of the vacuum chamber to complete the 4-button BPM system.

A simple relation between the output signals and the position information for a 4-button BPM is

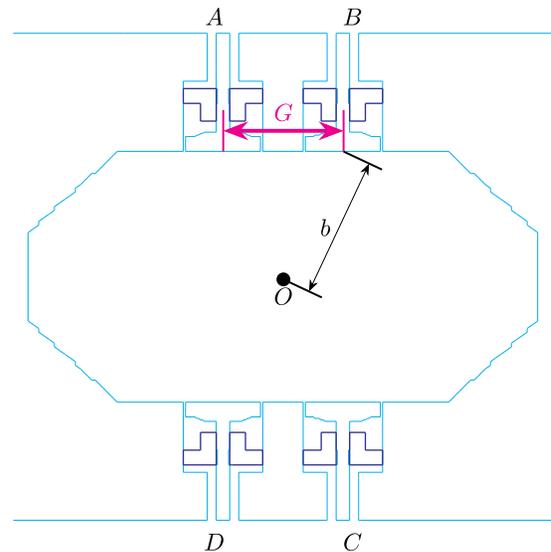


FIG. 1. Cross section layout of the SSRF 4-button BPM pickup.

<sup>\*</sup>chenzhichu@sinap.ac.cn  
<sup>†</sup>yuanrenxian@sinap.ac.cn

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$$dQ_B(t) = \rho dx \int_a^b \frac{I_b(z, t)}{c_0} dz, \quad (3)$$

where  $dQ_B$  is the induced charge on the button,  $\rho$  is the linear charge density,  $I_b(z, t) = \frac{Q_0}{\sqrt{2\pi\sigma_t}} \exp[-\frac{(t-z/c_0)^2}{2\sigma_t^2}]$  is the longitudinal current distribution of the Gaussian bunch and  $c_0$  is the speed of light. The induced current is the rate of change of the charge:

$$dI_B(t) = \rho[I_b(b, t) - I_b(a, t)]dx. \quad (4)$$

This means that the induced current on the button is proportional to the change of the current of the beam within the button area.

For a small circular button, the linear charge density of the induced charge is approximately linear to the

$x$ -coordinate:  $\rho(x) \simeq \rho + \alpha x$ . The induced current on the whole button could be obtained by integrating over the  $x$ -axis (as shown in Fig. 3):

$$I_B(t) = \int_{-r}^r \rho(x) \{I_b(b(x), t) - I_b[a(x), t]\} dx. \quad (5)$$

For a circular electrode (as shown in Fig. 3), the induced current is

$$I_B(t) = \int_0^\pi (\rho + \alpha r \cos \theta) \times [I_b(r \sin \theta, t) - I_b(-r \sin \theta, t)] r \sin \theta d\theta.$$

Thus the induced current in the frequency domain can be written as

$$\begin{aligned} I_B(\omega) &= I_b(\omega) \int_{-\pi}^0 (\alpha r \cos \theta + \rho) \left[ 1 - \exp\left(\frac{2j\omega r \sin \theta}{c_0}\right) \right] r \sin \theta d\theta \\ &= I_b(\omega) \rho r \left[ -2 - \int_{-\pi}^0 \sin \theta \exp\left(\frac{2j\omega r \sin \theta}{c_0}\right) d\theta \right] \\ &= I_b(\omega) \rho r \left[ -2 - j\pi J_1\left(\frac{2\omega r}{c_0}\right) + \pi H_{-1}\left(\frac{2\omega r}{c_0}\right) \right], \quad \text{for } \frac{2\omega r}{c_0} \in \mathbb{R}, \end{aligned} \quad (6)$$

where  $r$  is the radius of the electrode.  $J_1$  and  $H_{-1}$  denote the Bessel function of the first kind and the Struve function, respectively, where  $J_\nu(z)$  satisfies

$$z^2 y'' + zy' + (z^2 - \nu^2)y = 0,$$

and  $H_\nu(z)$  satisfies

$$z^2 y'' + zy' + (z^2 - \nu^2)y = \frac{2}{\pi} \frac{z^{\nu+1}}{(2\nu - 1)!}.$$

To simplify the calculation, the electrode is regarded as a rectangle whose sides are  $2r/\kappa$  and  $\kappa\pi r/2$ , where  $\kappa$  is a constant and is chosen to be 1 in this case, when the bunch length is larger than or approximately equal to the radius of the electrode. In that case, the induced current can be written as:

$$I_B(\omega) \simeq \rho \frac{\kappa\pi r}{2} \left[ 1 - \exp\left(\frac{2j\omega r}{\kappa c_0}\right) \right] I_b(\omega). \quad (7)$$

The induced current of the BPM electrode  $I_B(\omega)$  will be released through the  $50 \Omega$  load and the capacitor of the electrode, as shown in the equivalent circuit in Fig. 4 inspired by [10]. The input voltage of the BPM electrode thus could be written as:

$$U_B(\omega) = I_B(\omega) \frac{R + j\omega L}{1 - \omega^2 LC + j\omega CR}, \quad (8)$$

where  $R = 50 \Omega$  is the load and  $C$  the capacitance between the electrode and the ground which is in the range of 1 pF and 10 pF depending on the size and geometry of the button in most cases. The capacitive reactance is far greater than the resistance of the load at the working frequency, 500 MHz at the SSRF, of the electronics of the BPM, so the output voltage is primarily contributed by the resistor

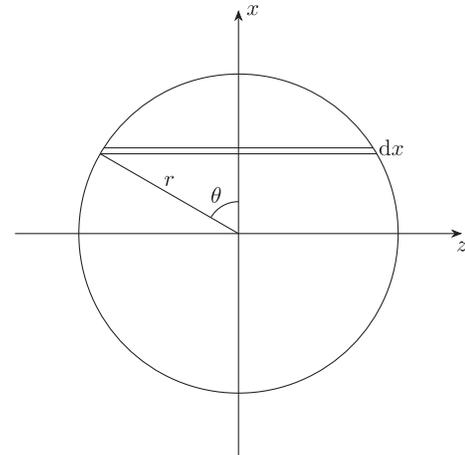


FIG. 3. Induced current on a circular button.

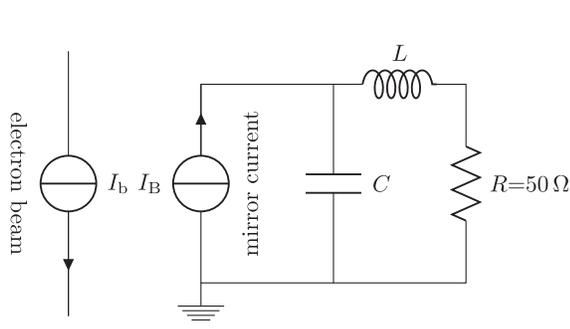


FIG. 4. Equivalent circuit.

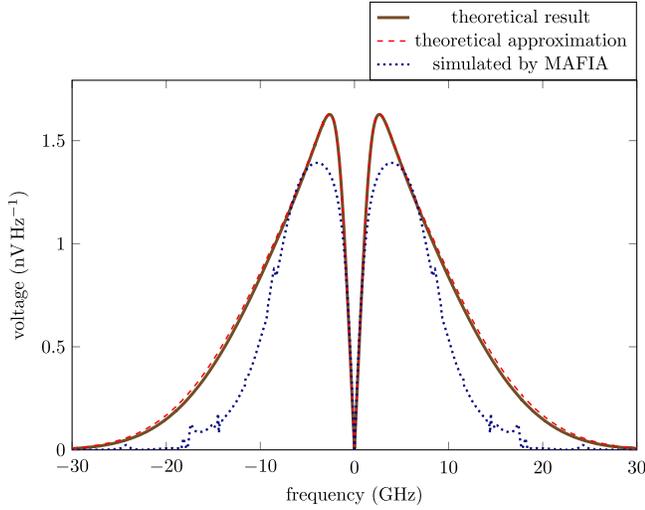


FIG. 5. Output spectra of the BPM electrode simulated by MAFIA and calculated with Eq. (8).

*R.* Therefore, the capacitance is negligible when estimating resolution of the BPM electrodes.

The calculated spectrum [using Eq. (8) and assuming  $L = 2.3$  nH and  $C = 2.2$  pF] of the output signal of the BPM electrode and the simulated one (using MAFIA) are plotted in Fig. 5. The power and the SNR of the signals at different beam currents to be input to the BPM electronics are listed in Table II.

TABLE II. The power and the SNR of the signals at different beam currents to be input to the BPM electronics (10 MHz bandwidth).

| Beam current (mA) | $P$ (dBm) | SNR (dB) |
|-------------------|-----------|----------|
| 0.2               | -64.4     | 66.4     |
| 0.7               | -54.0     | 76.8     |
| 1                 | -50.7     | 80.1     |
| 10                | -30.7     | 100.1    |
| 100               | -10.7     | 120.1    |
| 300               | -1.2      | 129.6    |
| 400               | 1.3       | 132.1    |

As noticed, the magnitude of the simulation result does not agree with the theoretical one thoroughly. The lumped-parametric model does not qualify on all frequencies, but the results are close enough in practice.

#### IV. WAKEFIELD IMPEDANCE

The output signal of the BPM electrode should be large, to improve the resolution. However, to achieve large signal levels requires physical large area electrodes and wide gap dimensions, which can lead to substantial wakefield effects, and contribute to beam instabilities, as well as to local RF heating effects in the BPM electrodes.

The beam coupling, or wakefield impedance has been studied in detail, so that the dimensions of the BPM electrode can be optimized during the design stage. Based on impedance formulas [11–13] and inspired by the lumped model method [10], a new model was established which not only can determine the dimensions of the electrode—such as the gap between the button and the vacuum chamber, the diameter and the thickness of the button—during the design stage, but also provide an approach to estimate its coupling impedance.

A wakefield is generated when the beam passes the electrodes. The real (resistive) part of the equivalent longitudinal wake-impedance corresponds to the energy loss of the beam, and the imaginary (reactive) part is related to the energy stored in the capacitance of the button electrode, i.e., the virtual work. In case of short range wake fields caused by a broadband button electrode, the imaginary part of the wake-impedance is responsible for the energy exchange between head and tail of the bunch. Even though this effect does not cause power losses to the beam bunch, it drives a longitudinal oscillation between bunch head and tail, thus may cause head-tail instabilities of a bunch or multi-bunch coupling instabilities under certain circumstances.

From Eqs. (7) and (8), the consumed power spectrum density [7,10] of the induced current can be written as the follows, considering only transverse field components of the beam passing the electrode:

$$\begin{aligned}
 P_B(\omega) &= I_B^*(\omega) U_B(\omega) \\
 &= |I_b(\omega)|^2 2\kappa^2 \rho^2 r^2 \\
 &\quad \times \left[ 1 - \cos\left(\frac{\omega}{\omega_B}\right) \right] \frac{R + j\omega(L - \omega^2 L^2 C - R^2 C)}{(1 - \omega^2 LC)^2 + (\omega CR)^2},
 \end{aligned} \tag{9}$$

where  $\omega_B = c_0/2\kappa r$  is the characteristic frequency of the electrode. The real part of the right-hand side of Eq. (9) expresses the energy loss of the induced current on the load and the imaginary part is the capacity of the energy stored in the capacitance of the button electrode. The energy losses of the beam due to the wakefield is the real part of the following coupling power spectrum density:

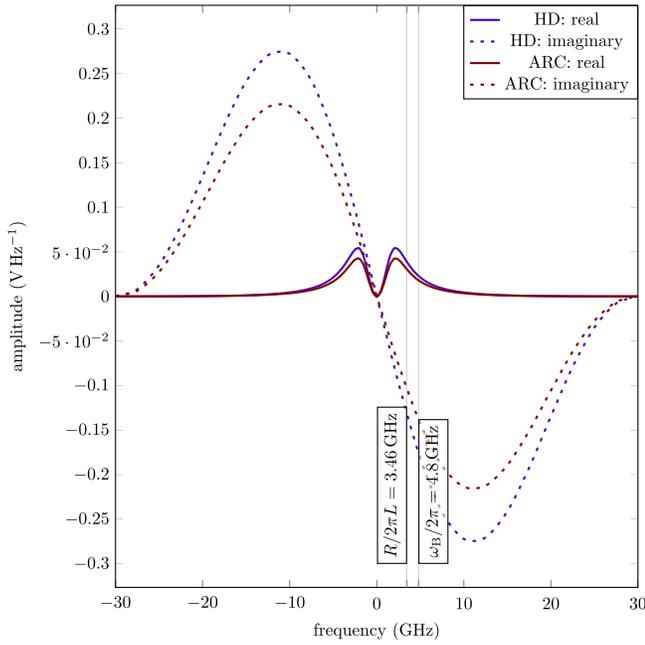


FIG. 6. Wakefield impedance spectra of a single button.

$$P_c(\omega) = I_b^*(\omega) \cdot [I_b(\omega)Z(\omega)] = |I_b(\omega)|^2 Z(\omega), \quad (10)$$

where  $Z(\omega)$  is the wakefield impedance of the BPM. Since only the real part of  $Z(\omega)$ , contributes for energy consumption, the energy loss of the beam has to be equal to the work on the load resistance. Define  $Z_R(\omega)$  as the longitudinal wakefield impedance which comes from the load. Comparing the real parts of Eqs. (9) and (10), the real part of  $Z_R(\omega)$  is expressed as:

$$\Re[Z_R(\omega)] = \frac{2\kappa^2 \rho^2 r^2 [1 - \cos(\omega/\omega_B)]}{(1 - \omega^2 LC)^2 + (\omega CR)^2} R. \quad (11)$$

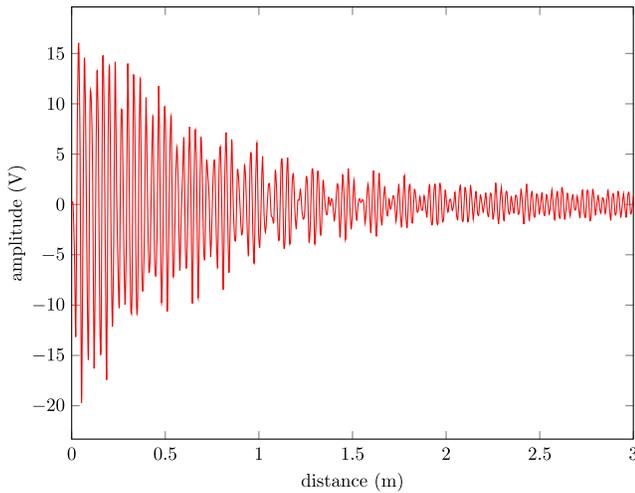


FIG. 7. The longitudinal wakefield potential of the BPM simulated by MAFIA.

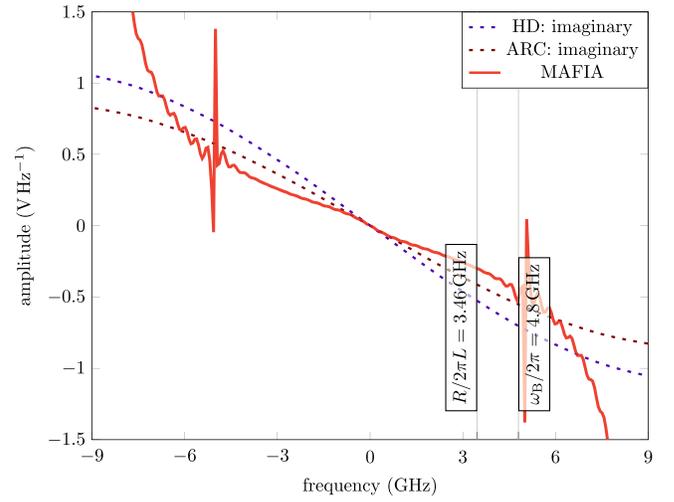


FIG. 8. Spectrum of the longitudinal wakefield potential of the HD-BPM simulated by MAFIA. The analytically calculated ones are listed for comparison. The results shown in Fig. 6 have been multiplied by 4 since there are four buttons in a BPM.

The longitudinal wake-impedance is the Fourier transformation of the time domain wakefield. The real and the imaginary part of the analytic function  $Z_R(\omega)$  satisfies the following Hilbert transform relation: [10,14]

$$\Im[Z_R(\omega)] = -\frac{1}{\pi} \text{p.v.} \int_{-\infty}^{\infty} \frac{\Re[Z_R(\omega')]}{\omega - \omega'} d\omega', \quad (12)$$

where p.v. stands for the Cauchy principal value.

Considering the fact, that the effective load impedance for the induced current on the button electrode is bandwidth limited, the limits of the integral in Eq. (12) can be reduced to a range  $[-R/L, R/L]$ , which results to the imaginary part of the wakefield impedance due to the load:

$$\Im[Z_R(\omega)] = -\frac{\kappa^2 \rho^2 r^2 \sin(\omega RC)}{\omega_B^2 R^2 C^2 [1 + (\omega RC)^2]} R. \quad (13)$$

As the capacitance of the load circuit does not consume energy, the real part of that contribution to the wake-impedance equals to zero. By comparing the imaginary parts of Eqs. (9) and (10), the imaginary part of this part of the impedance can be written:

$$Z_C(\omega) = 2\kappa^2 \rho^2 r^2 \left[ 1 - \cos\left(\frac{\omega}{\omega_B}\right) \right] \frac{\omega(L - \omega^2 L^2 C - R^2 C)}{(1 - \omega^2 LC)^2 + (\omega CR)^2}. \quad (14)$$

Thus the total impedance  $Z(\omega)$  is obtained:  $Z(\omega) = Z_R(\omega) + jZ_C(\omega)$ .

From these results it turns out, for bunch lengths substantially larger than the diameter of the electrode, i.e., the beam spectrum is well below the characteristic frequency of the electrode, the imaginary part of the

TABLE III. The results of the wakefield impedances when varying the button thickness.

| Parameter                         | Button thickness (mm) |        |        |        |        |
|-----------------------------------|-----------------------|--------|--------|--------|--------|
|                                   | 1                     | 2      | 3      | 4      | 5      |
| adjusted capacitance (pF)         | 1.56                  | 2.20   | 3.09   | 3.85   | 4.61   |
| impedance@1.5 GHz (MAFIA)         | 0.35                  | 0.234  | 0.18   | 0.165  | 0.143  |
| effective inductance (nH) (MAFIA) | 0.0262                | 0.0183 | 0.0148 | 0.0124 | 0.0101 |
| impedance@1.5GHz (model)          | 0.349                 | 0.236  | 0.178  | 0.143  | 0.12   |
| effective inductance (nH) (model) | 0.0248                | 0.0168 | 0.0127 | 0.0102 | 0.0085 |

wake-impedance contribution is mainly caused by the resistive load impedance [11,12], see Eq. (13). On the other hand, for bunch lengths substantially shorter than the diameter of the electrode, the wake-impedance contribution is mainly caused by the capacitance of the equivalent load circuit, given in Eq. (14). In third generation light sources, such as the SSRF, the bunch length is typically of similar dimension as the electrodes of the BPM pickups. The beam spectrum often extends to frequencies of 10 GHz, or beyond.  $Z_C(\omega) < \Re[Z_R(\omega)]$  at low frequencies  $\omega < R/L$  and  $Z_C(\omega) > \Re[Z_R(\omega)]$  at high frequencies. For our typical bunch length (4.2 mm or 14 ps) at the SSRF the wake-impedance has to be determined by the external load as well as the capacitance of the electrode, i.e., Eqs. (11), (13), and (14), and none of them should be ignored.

Based on the above results, related calculations and simulations have been performed at the SSRF. After some simple computations, the capacitance of the button electrode was estimated to be 1.9 pF. The capacitance and the inductance of the ceramic section, required to seal the vacuum, was estimated with 0.5 pF and 2.3 nH, respectively. So the values of the equivalent circuit total to 2.4 pF and 2.3 nH, respectively. The capacitance was later adjusted to 2.2 pF based on our measurements.

Figure 6 shows, at low frequencies, i.e.,  $\omega < R/L$ , the wake-impedance is dominated by the external load. At  $|\omega| \ll \omega_B$ , the imaginary part is proportional to the frequency. At those low frequencies, the broadband impedance  $|Z(\omega)/n|$  ( $n = \omega/\omega_{\text{rev}}$  is the harmonic number) of a single HD-BPM electrode computes to  $27.3 \mu\Omega$ , so the total impedance for the BPM with four electrodes is  $109.2 \mu\Omega$ , and the equivalent inductance is 0.0250 nH. As at higher frequencies, the wake-impedance does not follow this linear factor with frequency, the effective longitudinal coupling impedance [[15], Eq. (5)][[16], Eq. (2.1)] was modified to match the computations, using an equivalent inductance of 0.0168 nH.

Figure 7 shows the time domain longitudinal wake potential of a MAFIA simulation of our BPM. The real and the imaginary parts of the equivalent wake impedance are derived simply by a Fourier transformation [17]. The imaginary part of the spectrum in Fig. 8 was obtained directly from the wake potential, which fits to an effective longitudinal coupling impedance of  $102.2 \mu\Omega$ , 0.0183 nH.

The simulated and calculated spectra show a reasonable agreement for  $|\omega| < 7$  GHz ignoring the HOM effects.

As the height of the arc BPM vacuum chamber is larger than that of the HD-BPM, the comparison of both cases for the longitudinal wake-impedances are shown in Fig. 6. For the arc BPM the broadband impedance at low frequencies and the effective longitudinal coupling impedance, based on our model, are found to be 0.0196 nH and 0.0132 nH, respectively, while the MAFIA simulation returns 0.0137 nH as effective longitudinal coupling impedance.

Further studies of the wake-impedance for button electrodes of different thickness are summarized in Table III, using both the analytical model and the MAFIA simulation. The simulation results confirm, thinner buttons tend to have a higher wake-impedance.

## V. HIGHER ORDER MODE RESONANCES

The bunch length at the SSRF is 4.2 mm and the related frequency spectrum extends to 10 GHz and above. Beside the TEM signal transmission and the broadband wake potential, also narrow HOM resonances of the button electrode can be excited by the passing bunches, in particular the  $TE_{11}$  mode, which determines frequency and amplitude of the dominant narrow-band impedance, and was studied in theory [18–20] and by numerical simulations [21,22]. The BPM at the SSRF was simulated with MAFIA and two narrow-band resonant peaks could be observed, near 9 GHz and 10.7 GHz, with  $25 \Omega$  and  $14 \Omega$

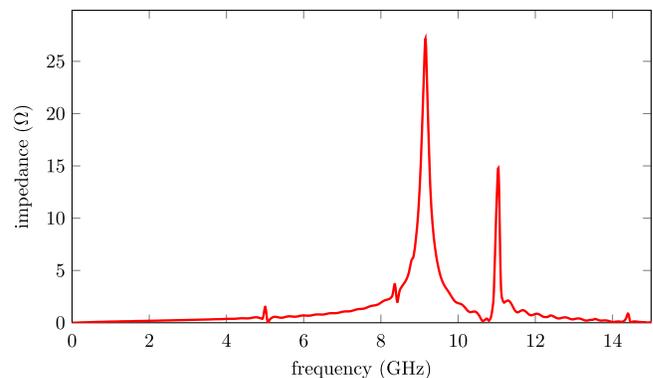


FIG. 9. Wakefield impedance of the BPM simulated in MAFIA shows the HOMs' influences.

TABLE IV. Calculated characteristic frequencies inside the electrode (denoted as  $f_{\text{electrode}}$ ) and cutoff frequencies of the vacuum chamber (denoted as  $f_{\text{cutoff}}$ ) of the HOMs.

| Mode number | $f_{\text{electrode}}$ (GHz) | $f_{\text{cutoff}}$ (GHz) |
|-------------|------------------------------|---------------------------|
| 1           | 5.4                          | 2.449                     |
| 2           | 9.1                          | 4.412                     |
| 3           | 10.7                         | 4.732                     |
| 4           | 12.15                        | 4.800                     |
| 5           | 12.24                        | 5.464                     |
| 6           | 14.48                        | 6.322                     |
| 7           | 14.52                        | 6.729                     |
| 8           | 15.23                        | 7.220                     |
| 9           | 15.31                        | 8.201                     |
| 10          | 17.29                        | 8.259                     |

impedance, respectively, see Fig. 9. The first resonance is related to the  $TE_{11}$  eigenmode of the electrode, the second is a higher order eigenmode, also listed in Table IV. One of the important BPM design criteria was to avoid any eigenmode excitation of the BPM pickup by the SSRF 500 MHz power RF fundamental frequency, and any of those higher order harmonics.

The TE modes trapped in the vacuum chamber will be coupled in the output signal of the electrode if eigenfrequencies are in the range of the working frequencies of the electronics [23,24], so the corresponding errors in position measurements should be considered. The cutoff frequency of the  $TE_{01}$  mode is substantially higher than the 500 MHz operation frequency of the signal processing electronics (see Fig. 9 and Table IV). The TE modes will not contribute significantly in position measurements.

### VI. IMPEDANCE MATCHING AND ELECTRODE CAPACITANCE

The induced current passes through a ceramic seal before it is extracted to the electronics (as shown in Fig. 10). This ceramic structure is used to seal the vacuum and impedance matching is required to avoid internal resonances. The impedance matching can be performed in two ways: changing the structure of the conductor [21,22] or changing the permittivities of the insulating medium [18]. The diameter of the neck of the feedthrough, where the ceramic seal is allowed to be expanded, was optimized by changing it from 0.92 mm to 1.5 mm. In the original design, the neck of the ceramic seal had a deviation of  $\pm 10 \Omega$  from the nominal  $50 \Omega$  characteristic impedance. The step response measured with a time-domain reflectometer (TDR) shows how the reflections could be reduced by modifying the dimensions of that neck (see Fig. 11).

Since the wavelengths of the frequencies of the beam signals are still large compared to the BPM electrode dimensions, the signal transmission is based on transverse electromagnetic (TEM) modes, allowing a straightforward calculation of the characteristic impedance.

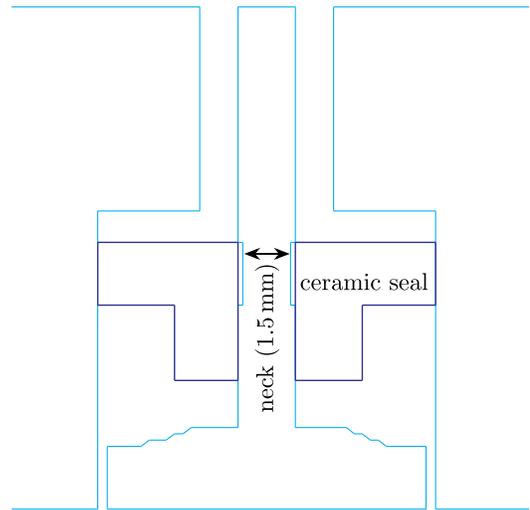


FIG. 10. The feedthrough structure of the SSRF BPM.

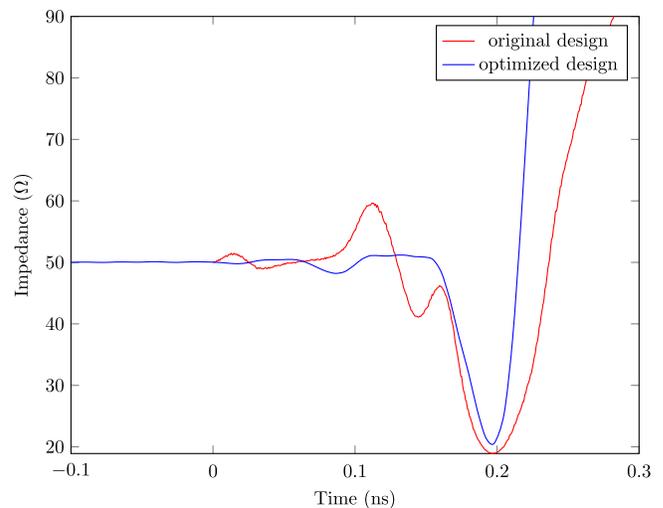


FIG. 11. Step response of the electrode measured at the SSRF. The radius of the neck in the original design is 0.92 mm and it's optimized to be 1.5 mm.



FIG. 12. The rise time of the open-circuit BPM.

The shunt capacitance electrode-to-ground is  $954 \text{ pFm}^{-1}$ . The effective permittivity of the upper part of the ceramic seal is 5.3 so the corresponding characteristic impedance is  $50.2 \text{ } \Omega$  and the shunt capacitance is  $150 \text{ pFm}^{-1}$ . The effective permittivity of the lower part of the ceramic seal is 2.55 so the corresponding characteristic impedance is  $66 \text{ } \Omega$  and the shunt capacitance is  $80 \text{ pFm}^{-1}$ . The total capacitance is  $2.4 \text{ pF}$  and is confirmed by measuring the rise time with a TDR. The result of the open-circuit probe is  $244 \text{ ps}$  (from 10% to 90%, as shown in Fig. 12), i.e., the equivalent capacitance is  $2.2 \text{ pF}$ , which is expected from the model.

## VII. CONCLUSIONS

The estimate of the impedance of the BPM electrode is essential in a modern accelerator. This article studies the feasibility of using a lumped-parameter model, with measurable circuit elements, in place of computer simulations in the design stage. The analytical approach will be able to fine-tune BPM design parameters quickly without having to iterate a time-consuming numerical calculation over parameter values.

The button-style BPM of the SSRF was analyzed in terms of transfer impedance and sensitivity, and with some additional focus on the wake-impedance. The wakefield results, based on the analytical model, derived from a simple equivalent circuit, showed a good agreement with the numerical simulations.

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- [1] Z. Zhao and H. Xu, in *Proceedings of the 9th European Particle Accelerator Conference, Lucerne, 2004* (EPS-AG, Lucerne, 2004) [<http://accelconf.web.cern.ch/AccelConf/e04/>].
  - [2] Z. Zhao, H. Xu, and H. Ding, in *Proceedings of the 21st Particle Accelerator Conference, Knoxville, TN, 2005* (IEEE, Piscataway, NJ, 2005), p. 214.
  - [3] J. Hou, S. Tian, M. Zhang, Y. Xu, and G. Liu, *Chin. Phys. C* **33**, 145 (2009).
  - [4] R. Yuan, Y. Leng, L. Yu, L. Han, and K. Ye, *Science China, Physics, Mechanics & Astronomy* **54**, S305 (2011).
  - [5] Y. Leng, W. Zhou, Y. Chen, K. Ye, R. Yuan, Y. Yan, Y. Zou, G. Huang, G. Zhao, Z. Chen, L. Yu, J. Chen, J. Yu, C. Yin, L. Zhao, and D. Liu, in *Proceedings of the 11th European Particle Accelerator Conference, Genoa, 2008* (EPS-AG, Genoa, Italy, 2008), p. 1080.
  - [6] G. Roberto Aiello, R. G. Johnson, D. J. Martin, M. R. Mills, J. J. Olsen, and S. R. Smith, in *AIP Conf. Proc.* **390**, 341 (1997).
  - [7] R. E. Shafer, *IEEE Trans. Nucl. Sci.* **32**, 1933 (1985).
  - [8] S. R. Smith, in *AIP Conf. Proc.* **390**, 50 (1997).
  - [9] T. Shintake, M. Tejima, H. Ishii, and J. ichi Kishiro, *Nucl. Instrum. Methods Phys. Res., Sect. A* **254**, 146 (1987).
  - [10] F. Marcellini, M. Serio, A. Stella, and M. Zobov, *Nucl. Instrum. Methods Phys. Res., Sect. A* **402**, 27 (1998).
  - [11] S. S. Kurennoy and G. V. Stupakov, *Part. Accel.* **45**, 95 (1994).
  - [12] S. S. Kurennoy, R. L. Gluckstern, and G. V. Stupakov, *Phys. Rev. E* **52**, 4354 (1995).
  - [13] S. S. Kurennoy, *IEEE Trans. Microwave Theory Tech.* **44**, 1109 (1996).
  - [14] Morse and Feshbach, *Methods of Theoretical Physics* (McGraw Hill, New York, 1953) p. 373.
  - [15] F. J. Sacherer, *IEEE Trans. Nucl. Sci.* **24**, 1393 (1977).
  - [16] B. Zotter, Report No. CERN/ISR-TH/80-03, 1980.
  - [17] R. Klatt, F. Krawczyk, W.-R. Novender, C. Palm, T. Weiland, B. Steffen, T. Barts, M. J. Brooman, R. Cooper, C. T. Mottershead, G. Rodenz, and S. G. Wipf, in *Proceedings of the 1986 Linear Accelerator Conference* (SLAC, Stanford, CA, 1986), p. 276 [SLAC-Report-303].
  - [18] T. Obina, T. Shintake, Y. H. Chin, and N. Akasaka, in *Proceedings of the Particle Accelerator Conference, Dallas, TX, 1995* (IEEE, New York, 1995).
  - [19] G. V. Stupakov and S. S. Kurennoy, *Phys. Rev. E* **49**, 794 (1994).
  - [20] F. Caspers and T. Scholz, *Part. Accel.* **51**, 251 (1996).
  - [21] C. K. Ng, T. Weiland, D. Martin, S. Smith, and N. Kurita, in *Proceedings of the Particle Accelerator Conference, Dallas, TX, 1995* (IEEE, New York, 1995), p. 2485.
  - [22] N. Kurita, D. Martin, S. Smith, C. Ng, M. Nordby, and C. Perkins, in *Proceedings of the Particle Accelerator Conference, Dallas, TX, 1995* (IEEE, New York, 1995), p. 2512.
  - [23] John Corlett, Cho-K. Ng, and Stephen R. Smith, in *Proceedings of the Particle Accelerator Conference, Vancouver, BC, Canada, 1997* (IEEE, New York, 1997), p. 2116.
  - [24] R. Lill, G. Decker, J. Hoyt, X. Sun, and J. Wang, in *Proceedings of the 14th Beam Instrumentation Workshop, Santa Fe, NM* (LANL, Los Alamos, 2010), p. 260.