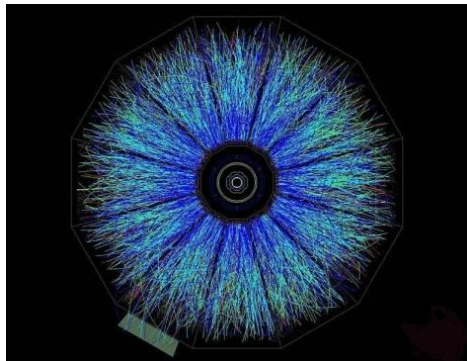


Higher Moments of Net-proton Multiplicity Distributions at RHIC



Xiaofeng Luo

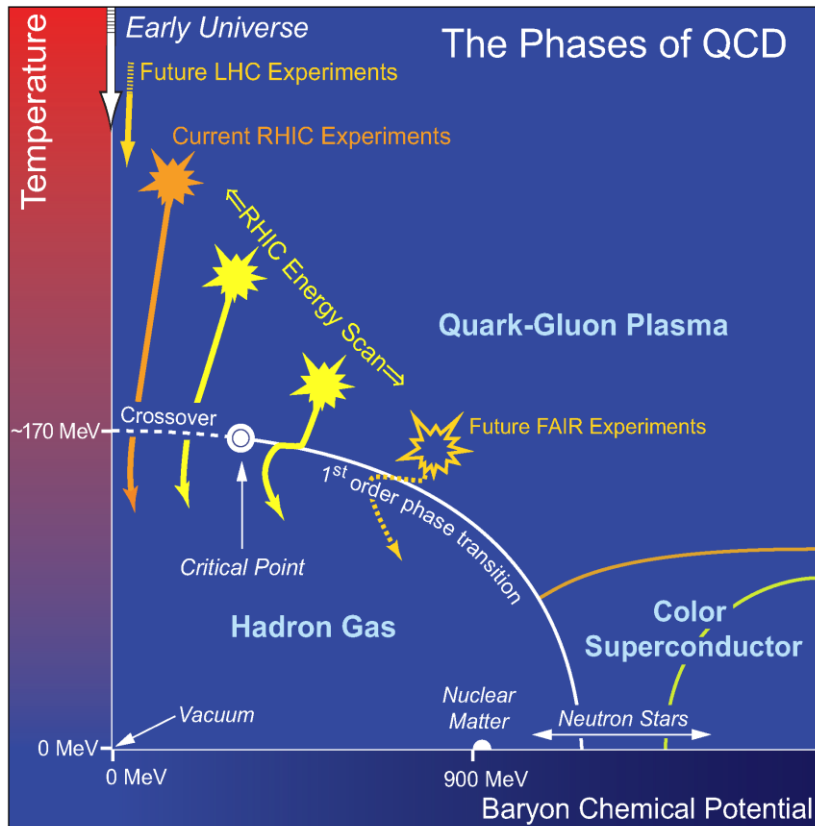
for the STAR Collaboration

*Institute of Particle Physics, Central China Normal University
University of Science and Technology of China*

7/18/2011

QCD Phase Diagram

Shows condition at which thermodynamically distinct phases can occur at equilibrium.



Lattice QCD:

➤ Crossover at $\mu_B = 0$, 1st order phase transition at large μ_B .

➤ QCD Critical Point: The end point of first order phase transition boundary.

Y. Aoki et al., Nature 443:675-678, 2006

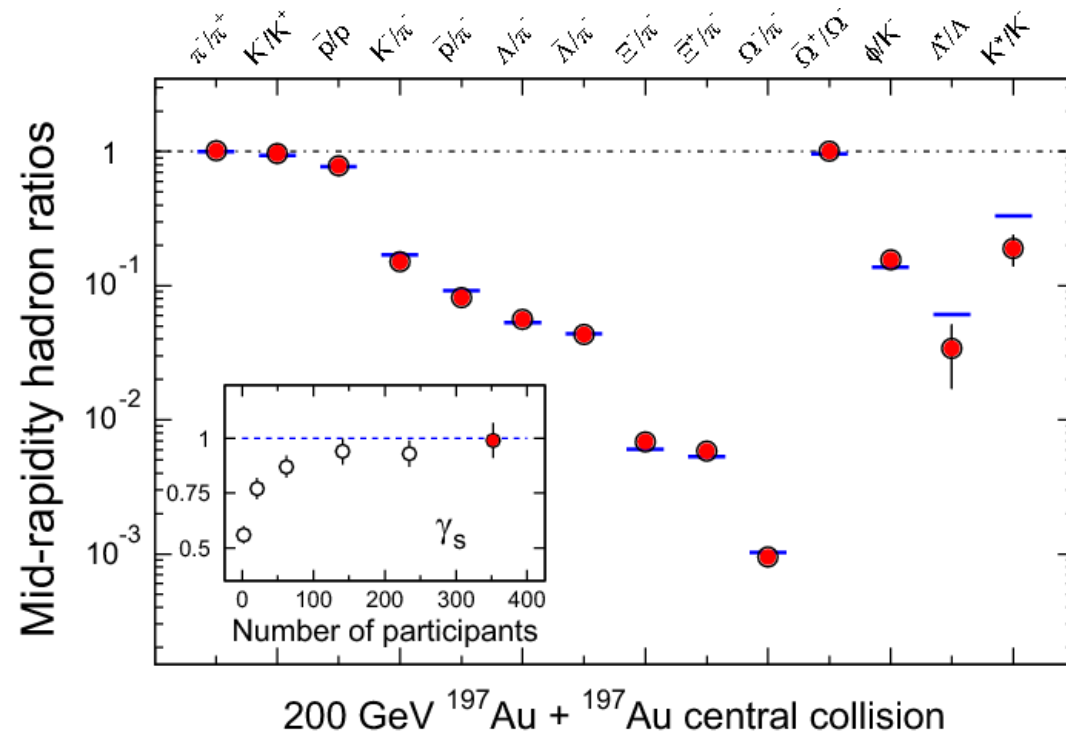
Motivations:

➤ Map the QCD Phase Boundary.

➤ Search for the QCD Critical Point.

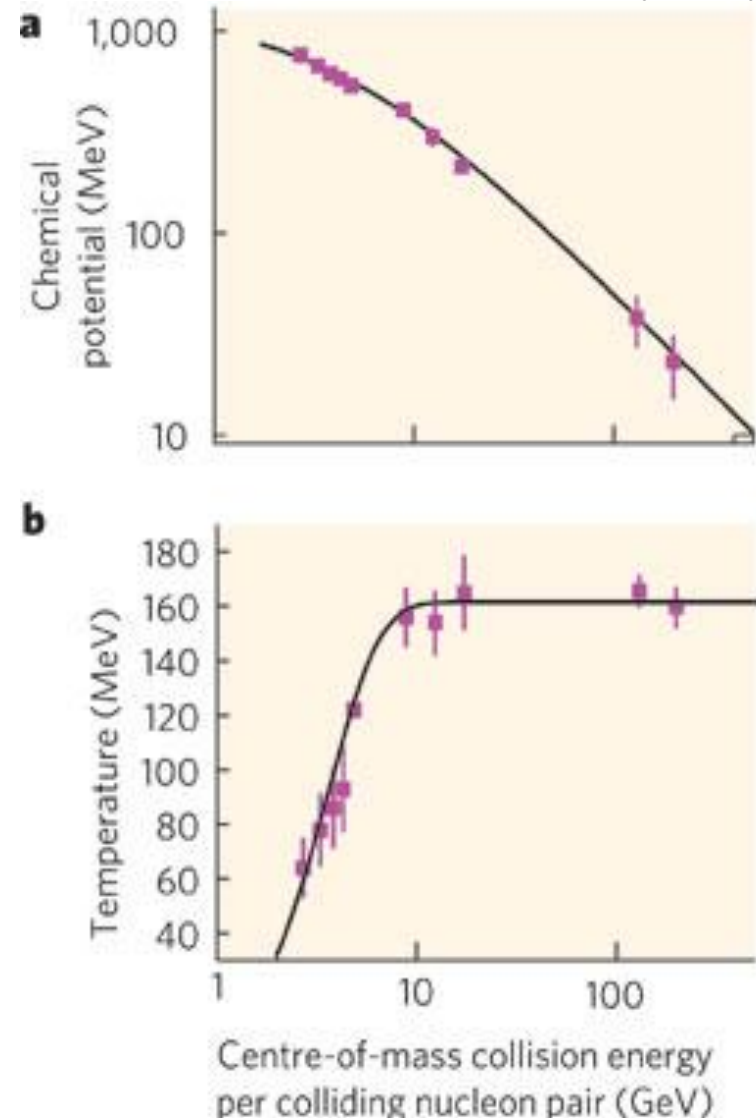
Statistical Particle Production

- Particle ratio fit with Thermal Model: Chemical freeze out temperature (T) and baryon chemical potential (μ_B). Nucl. Phys. **A757**,102 (2005);



- Varying the colliding energy, we can access different regions (T, μ_B) on the QCD phase diagram.

Nature 448:302-309 (2007)

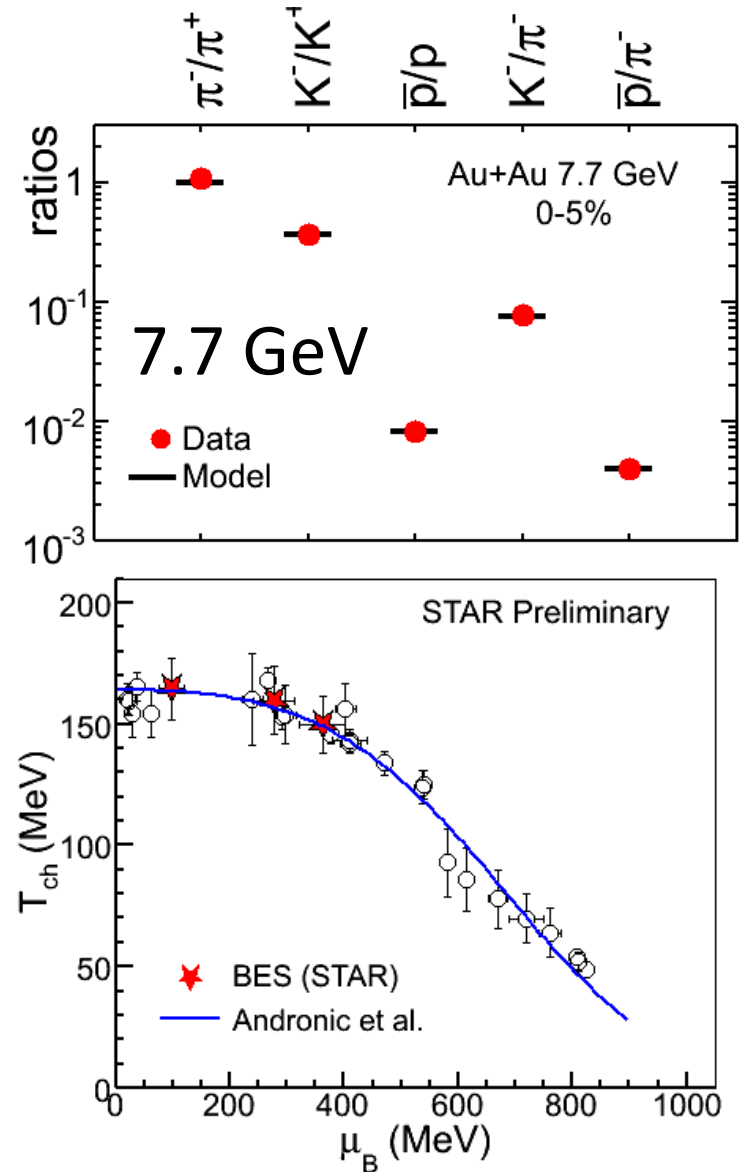


Access the QCD Phase Diagram

➤ RHIC Beam Energy Scan (BES) Program.

$\sqrt{s_{NN}}$ (GeV)	Good events in Million MB
5.0	?
7.7	~ 5
11.5	~ 11
19.6	~ 17
27	~ 33
39	~ 170

➤ STAR Detector : Large Uniform Acceptance. Ideal detector to perform fluctuation and correlation measurements.



Good opportunities to search for the QCD critical point ! QM2011 talk: Lokesh

Locating the QCD Critical Point

Theoretical Calculations:

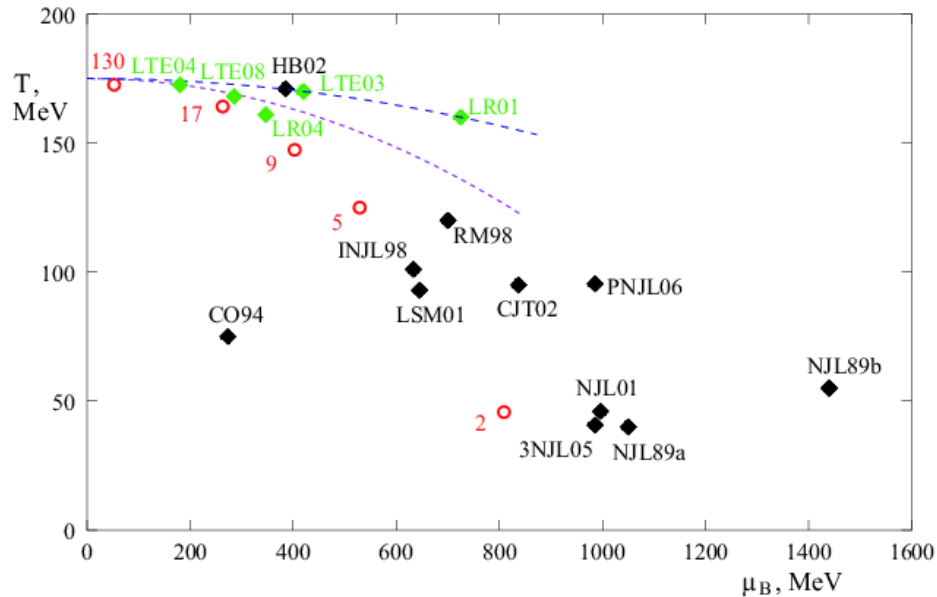
- Lattice QCD.
- QCD Based Models.

Vs

Experimental measurements

- Access the QCD Phase Diagram.
- Find Sensitive Observable.

Large uncertainties of theoretical calculation.



Signatures of QCD Critical Point:

- Diverge of the Correlation length (ξ)
- Non-Gaussian fluctuations.



Non-monotonic signal expected around QCD Critical Point.

M. Stephanov , Phys. Rev. Lett. 102, 032301 (2009)

M. Stephanov, PoSLAT2006:024,2006 (hep-lat/0701002)

Z. Fodor, S. D. Katz, hep-lat/0106002, het-lat/0401023.
hep-lat/0402006.

R. V. Gavai and S. Gupta, Phys. Rev. D 78, 114503 (2008).

Higher Moments: Non-Gaussian Fluctuation Measure

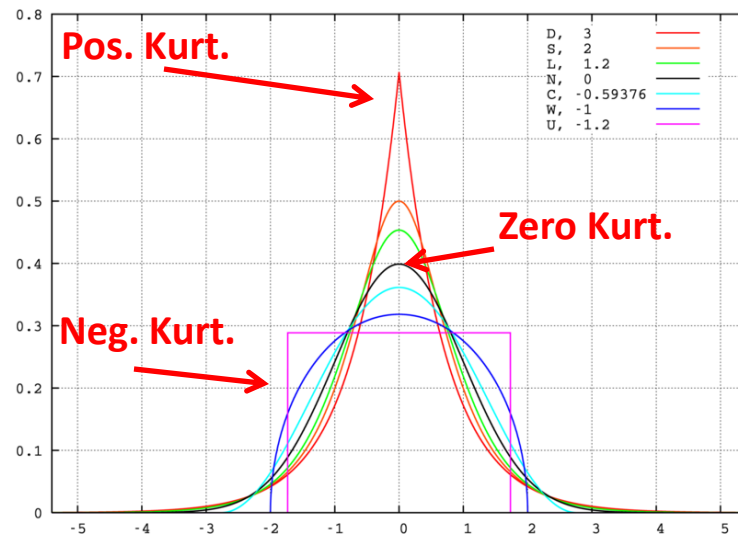
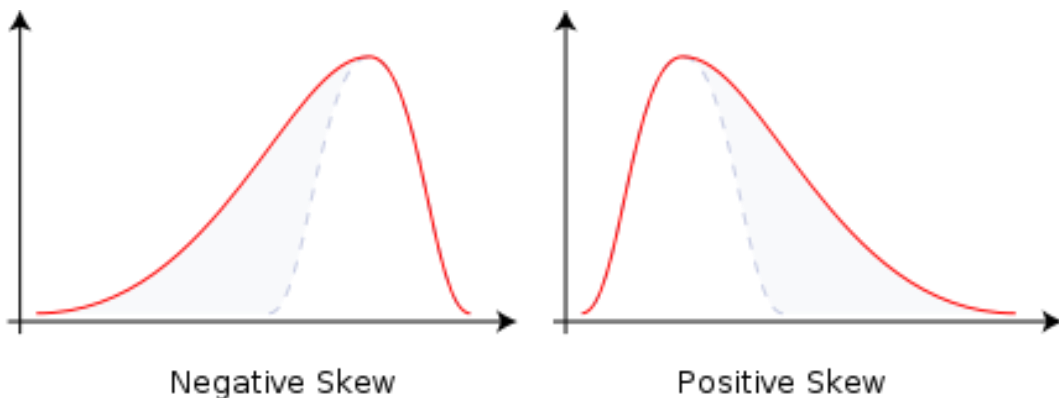
Definition : **N: Event by Event Multiplicity Distribution**

Mean: $M = \langle N \rangle$

St. Deviation: $\sigma = \sqrt{\langle (N - \langle N \rangle)^2 \rangle}$

Skewness: $s = \frac{\langle (N - \langle N \rangle)^3 \rangle}{\sigma^3}$

Kurtosis: $\kappa = \frac{\langle (N - \langle N \rangle)^4 \rangle}{\sigma^4} - 3$



➤ For Gaussian distribution, the skewness and kurtosis are equal to zero. **Ideal probe of the non-Gaussian fluctuations at CP.**

Importance of Higher Moments Method

➤ Link to Thermodynamic Susceptibilities in Lattice QCD and Hadron Resonance Gas (HRG) Model:

$$\chi_B^{(n)} = \left. \frac{\partial^n (P/T^4)}{\partial (\mu_B/T)^n} \right|_T$$

M.Cheng et al, Phys. Rev. D 79, 074505 (2009)

F. Karsch and K. Redlich, Phys. Lett. B 695, 136 (2011)

$$\chi_B^2 = \frac{1}{VT^3} \langle \delta N_B^2 \rangle$$

$$\chi_B^3 = \frac{1}{VT^3} \langle \delta N_B^3 \rangle$$

$$\chi_B^4 = \frac{1}{VT^3} (\langle \delta N_B^4 \rangle - 3 \langle \delta N_B^2 \rangle^2)$$

$$\chi_B^4 / \chi_B^2 = (\kappa \sigma^2)_B$$

$$\chi_B^3 / \chi_B^2 = (S \sigma)_B$$

Volume Cancel Out

Experimental measurable net-proton numbers fluctuations can reflect baryon and charge number fluctuations.

Y. Hatta et al, PRL 91, 102003 (2003)

➤ Sensitive to Correlation Length (ξ) : Sigma Model Calculations.

Due to finite size, finite time effects.
in heavy ion collisions. $\xi \sim 2-3$ fm.

$$\langle (\delta N)^2 \rangle \approx \xi^2$$

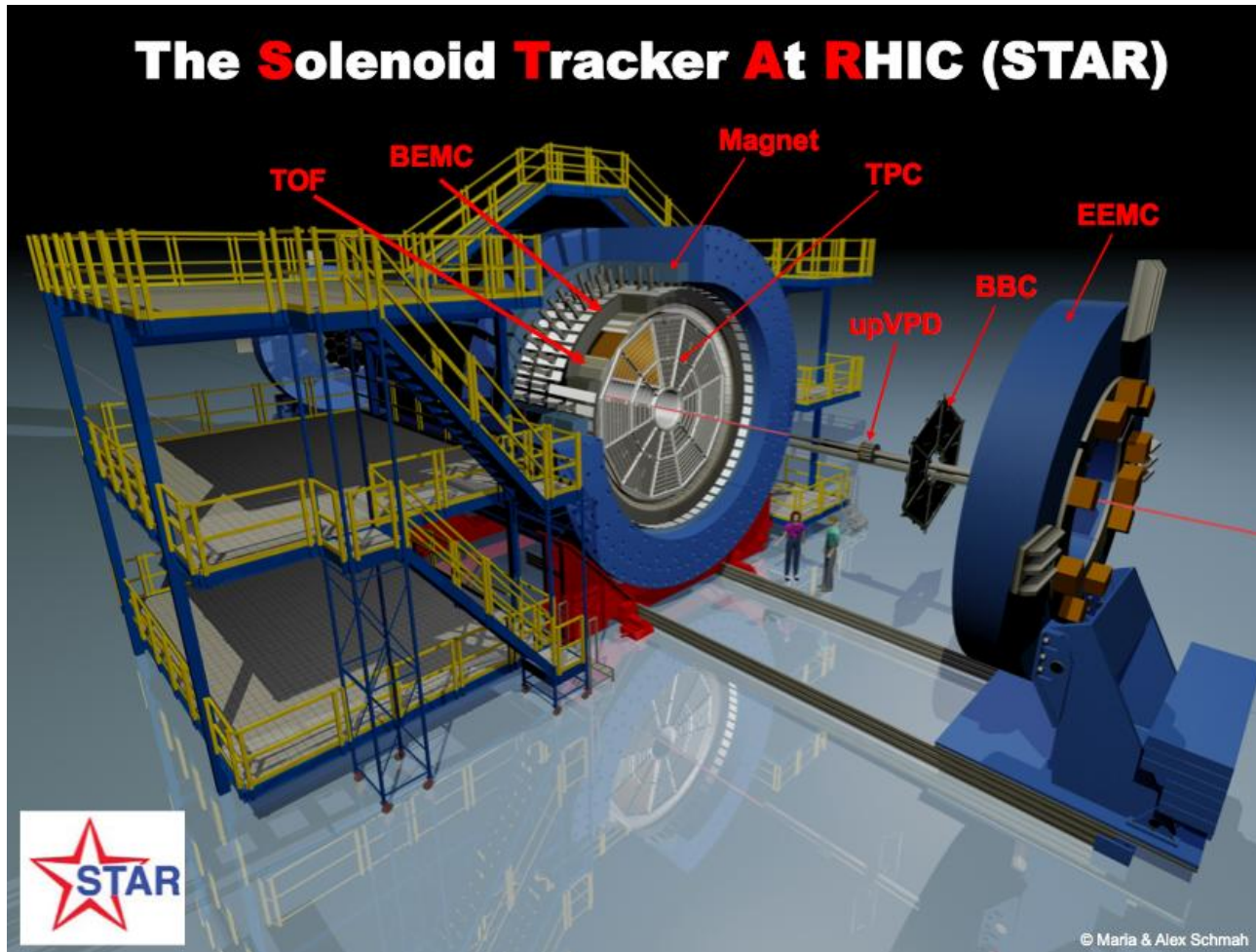
$$\langle (\delta N)^3 \rangle \approx \xi^{4.5}$$

$$\langle (\delta N)^4 \rangle - 3 \langle (\delta N)^2 \rangle^2 \approx \xi^7$$

M. A. Stephanov, Phys. Rev. Lett. 102, 032301 (2009)

C. Athanasiou, M. Stephanov, K. Rajagopal, Phys. Rev. D 82, 074008 (2010)

STAR Detector-3D Picture



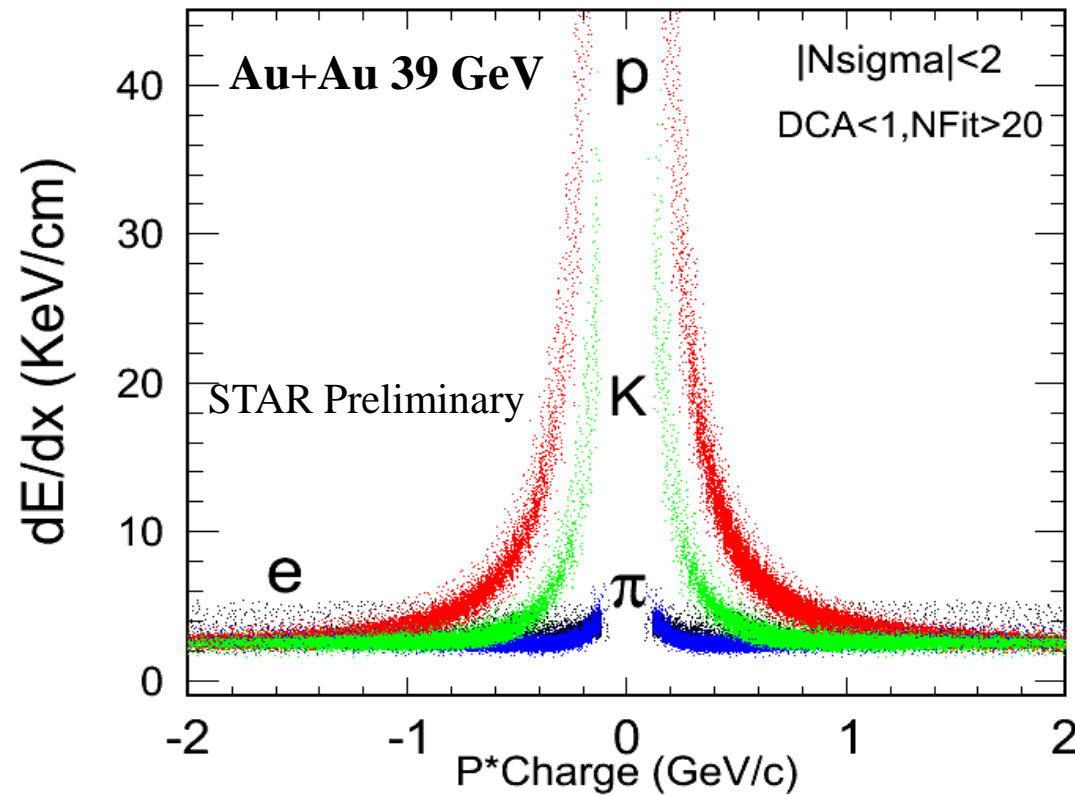
Time Projection Chamber:

- Acceptance: $-1 < \eta < 1$, $0 < \phi < 2\pi$
- Tracking: Particle momentum and trajectory.
- PID: Ionization Energy Loss (dE/dx).
(π , K) : $p_T < 0.7$, proton : $p_T < 1$ GeV/c

Time Of Flight: (Full install in Run 10)

- Acceptance: $-0.9 < \eta < 0.9$, $0 < \phi < 2\pi$
- Timing Resolution < 100 ps.
- PID: (π , K): $p_T < 1.6$, proton: $p_T < 3$ GeV/c

Particle Identification with TPC dE/dx



➤ Track Quality Cut:

$N_{\text{fits}} > 20$,
 $N_{\text{fits}}/N_{\text{FitPoss}} > 0.52$.
 $Dca < 1$ cm.

➤ PID Cut: dE/dx

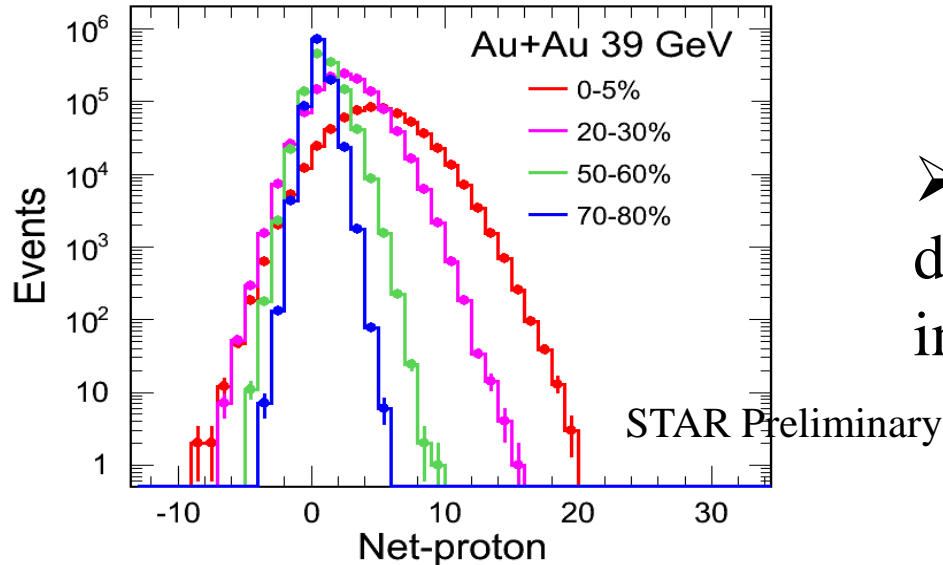
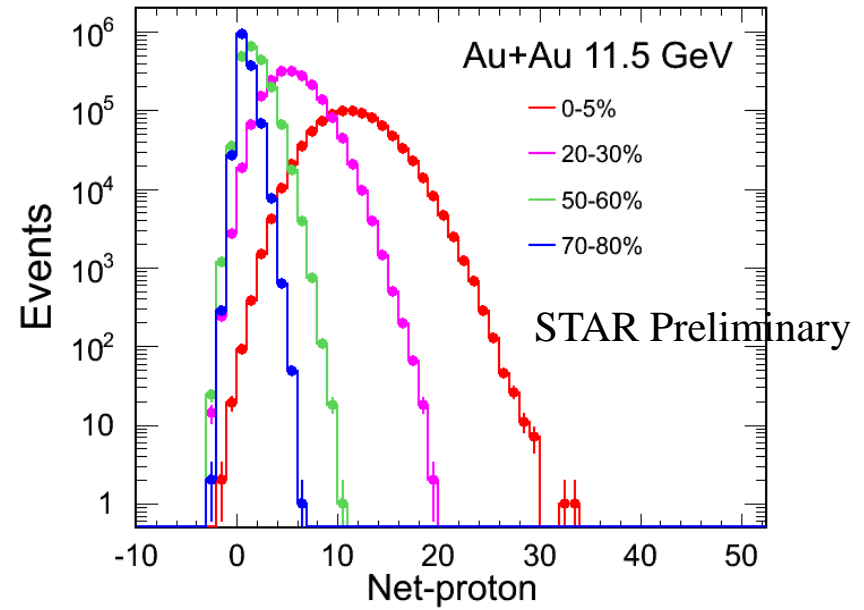
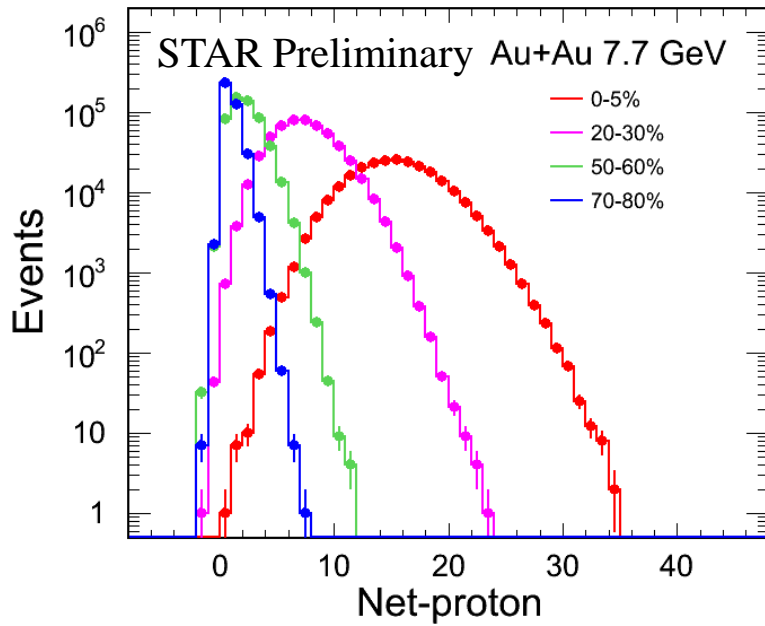
$|Z_p| < 2$

$$Z = \frac{\log[(dE/dx)|_{\text{measure}} / (dE/dx)|_{\text{theory}}]}{\sigma_E}$$

Within $0.4 < p_T < 0.8$ (GeV/c) and $|y| < 0.5$:

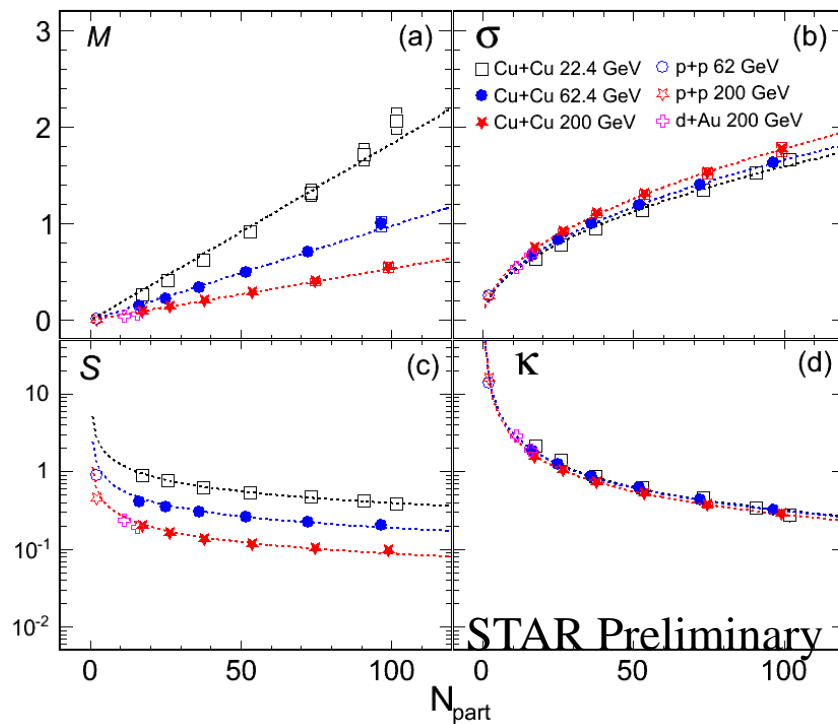
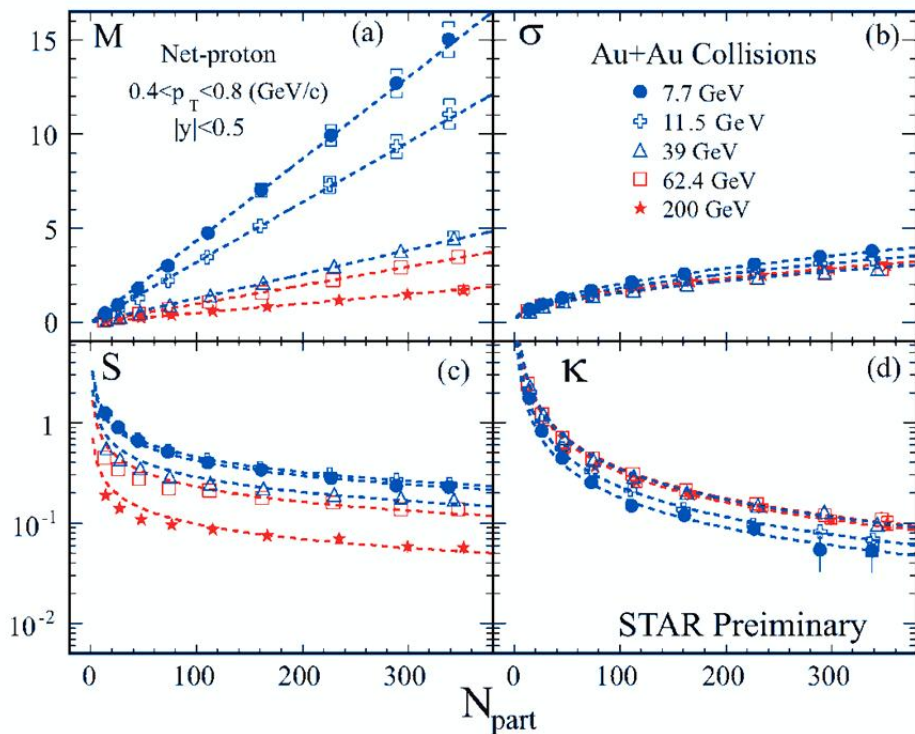
- Clean Proton and antiproton identification with TPC dE/dx .
- Similar efficiency for proton and anti-proton.

Event-by Event Net-proton Multiplicity Distributions



➤ The event-by-event net-proton distributions are more symmetrical in central collision than peripheral.

Centrality Dependence (I): Higher Moments



Central Limit Theorem (CLT)

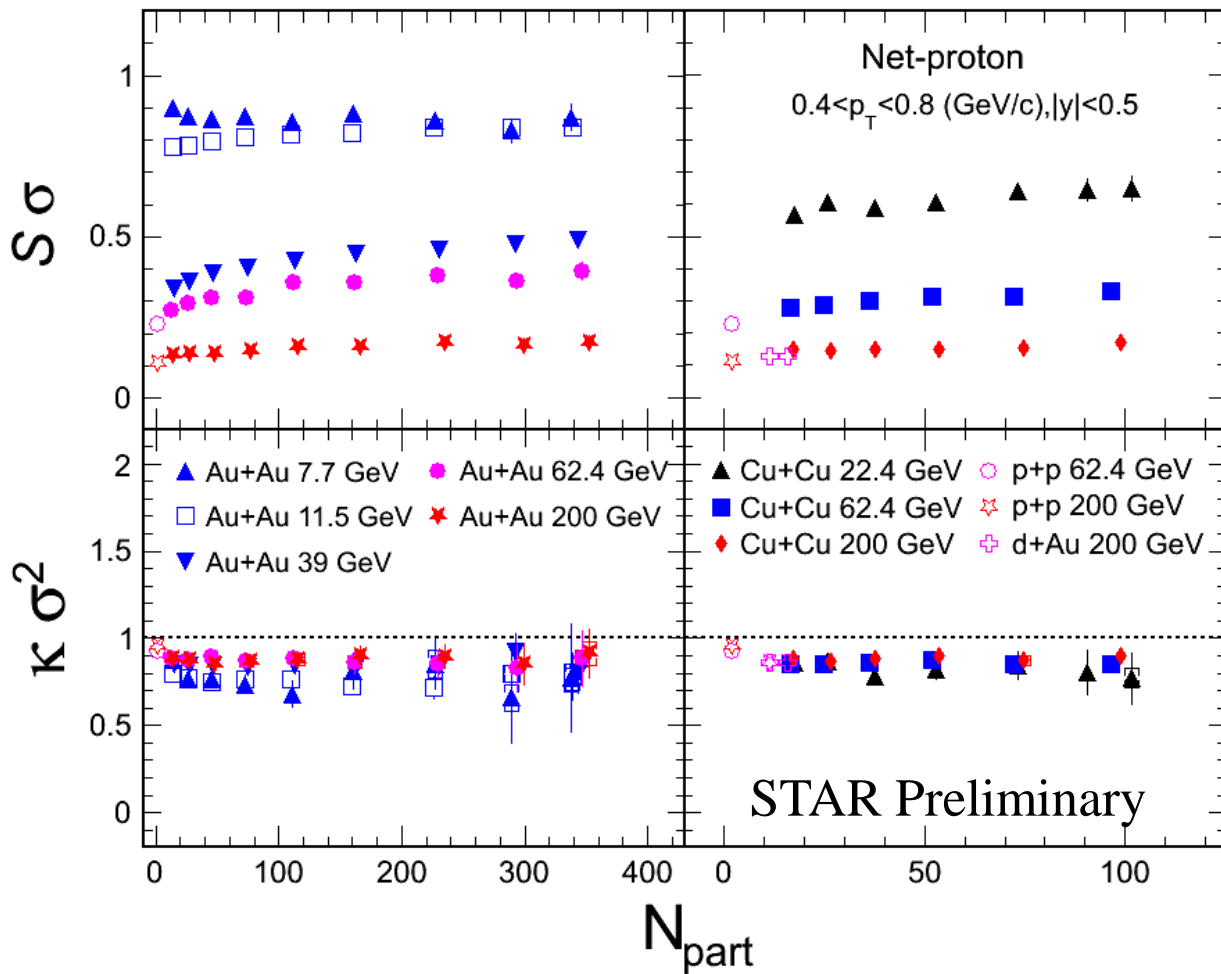
$$M_i = M_x \times C \times N_{part}, \sigma_i^2 = \sigma_x^2 \times C \times N_{part}$$

$$S_i = \frac{S_x}{\sqrt{C \times N_{part}}}, \kappa_i = \frac{\kappa_x}{(C \times N_{part})}$$

Consistent with CLT Expectations (lines).

Indicates many identical, independent particle emission sources.

Centrality Dependence (II): Moment Products



Related to baryon number susceptibility ratio:

$$(S\sigma)_B = \chi_B^3 / \chi_B^2$$

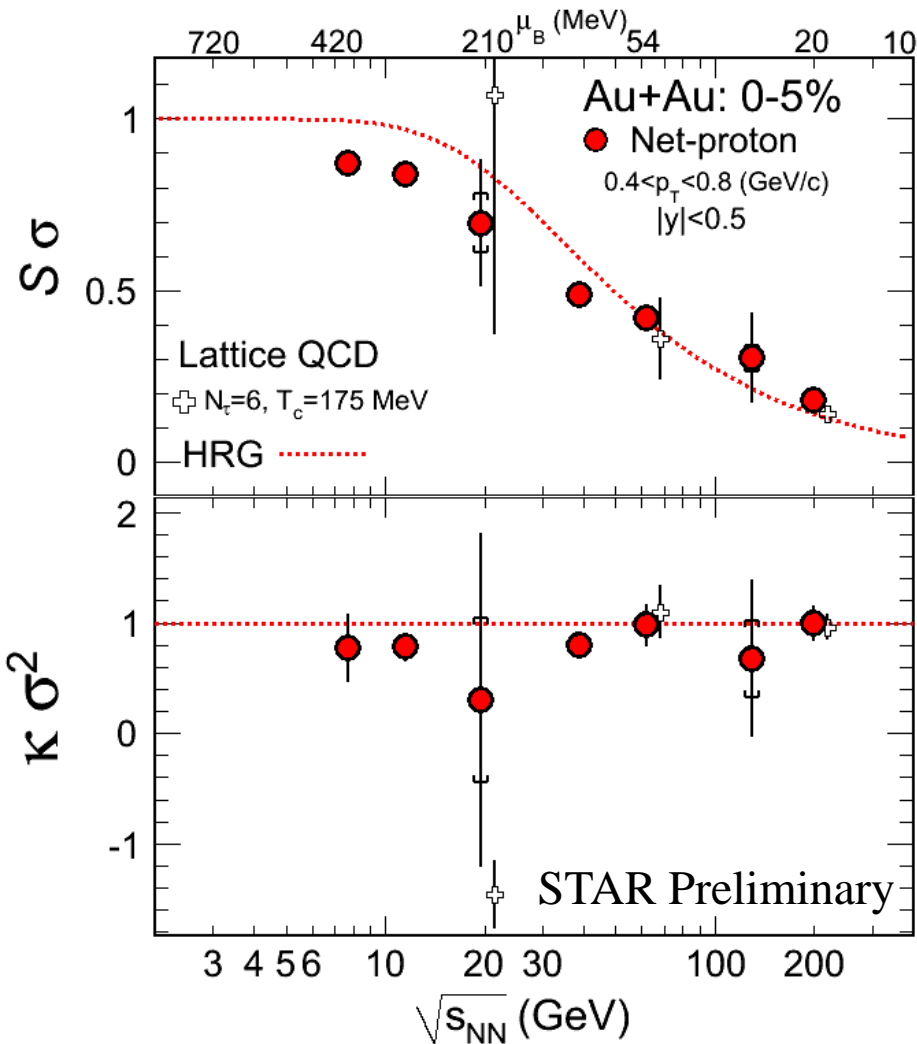
$$(\kappa\sigma^2)_B = \chi_B^4 / \chi_B^2$$

M.Cheng et al, Phys. Rev. D 79, 074505 (2009)

F. Karsch and K. Redlich, Phys. Lett. B 695, 136 (2011)

- $S\sigma$: Weak centrality dependence.
- $\kappa\sigma^2$: No centrality dependence.

Search for the QCD Critical Point



- Consistent with Lattice QCD and Hadron Resonance Gas (HRG) model at higher energies.
- Low energies (7.7, 11.5, 19.6 and 39 GeV) deviate from HRG model.

Reasons are still not clear :

1. Linked to the chiral phase transition and QCD critical point ?
2. Non-applicable of Grand Canonical Ensemble at low energy ?

B. Friman et al., arXiv:1103.3511

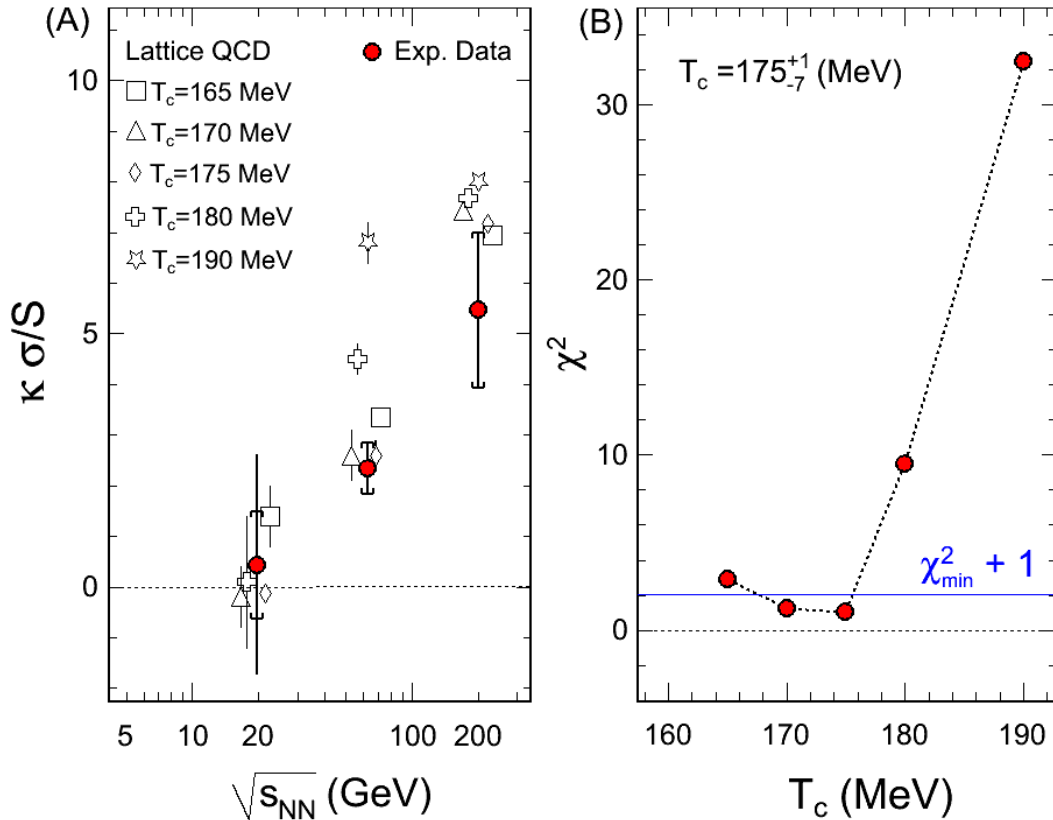
M. A. Stephanov, arXiv:1104.1627

R. Gavai and S. Gupta, Phys. Lett. B 696, 459 (2011)

F. Karsch and K. Redlich, Phys. Lett. B 695, 136 (2011)

B. Mohanty, QM 2011 talk , X. Luo QM2011 poster

Determining the Scale (T_c) for QCD Phase Diagram



➤ For the first time, direct comparison between experimental data with Lattice QCD.

➤ Open an new domain for probing bulk properties of nuclear matter.

➤ This temperature sets a scale of QCD phase diagram. We conclude that the phase transition temperature T_c at $\mu_B=0$ is **175 (+1) (-7) MeV**

$$\kappa \sigma / S = \chi_B^{(4)} / \chi_B^{(3)}$$

S. Gupta, X. Luo,
B. Mohanty, H. G. Ritter, N. Xu.
Science 332,1525 (2011)



Summary

- Higher moments are directly related to thermodynamic susceptibilities in Lattice QCD and HRG model. **It opens a new domain of probing bulk properties of nuclear matter and testing the non-perturbative QCD.**
- First time, the higher moments of net-proton distributions are used to **search for QCD critical point**. Deviations from HRG model are observed at low energies.
- First time, transition temperature T_c at $\mu_B=0$ is determined by comparing the experimental higher moments results with Lattice QCD results. We conclude that **$T_c=175 (+1) (-7)$ MeV.**

Outlook: 19.6 and 27 GeV high statistic data have been taken this year. New results will come soon.